## Meter : 3-phase to positive sequence polar


Meter : 3-phase to positive sequence polar .....  1
1 Description ..... 1
1.1 Pins ..... 1
1.2 Parameters ..... 1
1.3 Input ..... 1
1.4 Output ..... 1

## 1 Description

This device converts the first harmonic of the instantaneous value of 3 phase signals to the polar coordinates of the corresponding positive-sequence phasor in a reference frame rotating at the fundamental frequency.

### 1.1 Pins

This meter has five pins:

| pin | description |  | units |
| :---: | :---: | :---: | :---: |
| a | input pin | phase-a input signal | any |
| b | input pin | phase-b input signal | same as a |
| c | input pin | phase-c input signal | same as a |
| mag | output pin | magnitude of pos-sequence phasor | same as a |
| rad | output pin | angle of pos-sequence phasor | rad |

### 1.2 Parameters

The following parameter must be defined:

| parameter | description | units |
| :---: | :---: | :---: |
| freq | fundamental frequency of the input signal | Hz |

### 1.3 Input

The input pins may be connected to any control signals.
The 3 signals are the instantaneous values of a 3-phase quantity.

### 1.4 Output

The output is the polar phasor representation of the positive-sequence transformation of the instantaneous values of the 3-phase input signals. The polar coordinates are the magnitude and angle of that phasor in a reference frame rotating at the fundamental frequency.
The coordinates of the phasor in that reference frame are calculated over a sliding time window of period equal to $1 / f r e q$, as follows.
The ( $x, y$ ) coordinates of the first harmonic of each input signal $k$ are calculated as

$$
\begin{align*}
& x_{k}=\frac{2}{\text { period }} \cdot \int_{t-\text { period }}^{t} \operatorname{in}(t) \cdot \cos (2 \pi \cdot \text { freq } \cdot t) \cdot d t  \tag{1}\\
& y_{k}=\frac{2}{\text { period }} \cdot \int_{t-\text { period }}^{t}-i n(t) \cdot \sin (2 \pi \cdot \text { freq } \cdot t) \cdot d t
\end{align*}
$$

where the negative sign for $y$ follows the engineering convention for an inductive (lagging) current to have a negative angle when phasor rotation is counterclockwise.
The $(x, y)$ coordinates of the positive-sequence transformation are calculated as

$$
\begin{align*}
& \operatorname{seq} 1 \_x=\frac{1}{3} \cdot\left(x_{a}+r x_{b}+r^{2} x_{c}\right) \\
& \text { seq1 } y=\frac{1}{3} \cdot\left(y_{a}+r y_{b}+r^{2} y_{c}\right) \tag{2}
\end{align*}
$$

where $r$ represents a phasor rotation of $2 \pi / 3$, and $r^{2}$ a rotation of $4 \pi / 3$.
The conversion to polar coordinates is calculated as

$$
\begin{array}{ll}
\text { magnitude } & =\sqrt{\operatorname{seq} 1 \_x^{2}+\operatorname{seq} 1 \_y^{2}} \\
\text { angle } & =\tan ^{-1}\left(\frac{\operatorname{seq} 1 \_y}{\operatorname{seq} 1 \_x}\right) \tag{3}
\end{array}
$$

The phasor magnitude is the peak amplitude, not the RMS value. The phasor angle is expressed in radians.

