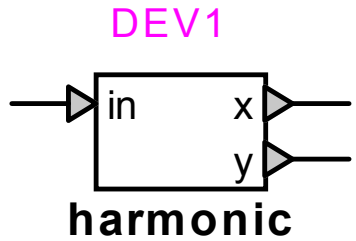


# Meter : harmonic x,y



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## 1 Description

This device converts the  $k$ -th harmonic of the instantaneous value of a signal to an  $(x,y)$  phasor representation. The  $(x,y)$  representation consists of the  $x$ - $y$  coordinates of the measured harmonic in a reference frame rotating at the fundamental frequency.

### 1.1 Pins

This meter has three pins:

<i>pin</i>	<i>type</i>	<i>description</i>	<i>units</i>
in	input pin	input signal	any
x	output pin	x-coordinate of $k$ -th harmonic phasor	same as input
y	output pin	y-coordinate of $k$ -th harmonic phasor	same as input

### 1.2 Parameters

The following parameters must be defined:

<i>parameter</i>	<i>description</i>	<i>units</i>
freq	fundamental frequency of the probed signal	Hz
k	index of the harmonic	

### 1.3 Input

The input pin may be connected to any control signal.

### 1.4 Output

The output is the  $(x,y)$  phasor representation of the  $k$ -th harmonic of the instantaneous value of the probed signal. The  $(x,y)$  coordinates are the  $x$ -axis and  $y$ -axis projections of that phasor on a reference frame rotating at the fundamental frequency.

The x-y coordinates of the phasor in that reference frame are calculated over a sliding time window of period equal to  $1/\text{freq}$ , as follows.

For  $k > 0$ ,

$$\begin{aligned}x &= \frac{2}{\text{period}} \cdot \int_{t-\text{period}}^t \text{in}(t) \cdot \cos(k \cdot 2\pi \cdot \text{freq} \cdot t) \cdot dt \\y &= \frac{2}{\text{period}} \cdot \int_{t-\text{period}}^t -\text{in}(t) \cdot \sin(k \cdot 2\pi \cdot \text{freq} \cdot t) \cdot dt\end{aligned}\tag{1}$$

where the negative sign for  $y$  follows the engineering convention for an inductive (lagging) current to have a negative angle when phasor rotation is counterclockwise.

For  $k = 0$ ,

$$\begin{aligned}x &= \frac{1}{\text{period}} \cdot \int_{t-\text{period}}^t \text{in}(t) \cdot dt \\y &= 0\end{aligned}\tag{2}$$